$... {\sf some of the} Secrets of cvc5$

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cvc5: SMT and beyond



cvc5: a Versatile and Industrial-Strength SMT Solver

- Architecture and the design of theory solvers
 - Focus on theory of strings
- Future Directions in cvc5
 - Deep restarts
 - Difficulty estimates



Architecture of cvc5



Architecture of cvc5



• Centralized methods for combining theories (Nelson-Oppen, polite)

Architecture of cvc5



- Eq reasoning, interface to T-combination managed by an *equality engine*
 - Standardized, mandatory for theories

Design of Theory Solvers in cvc5

- Kinds file and type checker
 - Defines the signature of the theory T
- Rewriter
- Theory solver
 - Maintains an equality engine
 - Manages theory combination, T-propagation
 - Given calls to check a set of T-literals $\ensuremath{\mathbb{M}}$:
 - Return a subset of M that is T-unsat (conflict clause)
 - Return a T-valid lemma
 - Return a model for the variables of $\ensuremath{\mathbb{M}}$

 \Rightarrow In this talk: the theory solver for strings and regular expressions

Designing the cvc5 Strings Solver

Strings and RegExp: Theoretical Challenges



• Many applications require *extended string functions* and *RegEx memberships*

• ctn(x, "a"), to_lower(x)="abc", x∈range("A", "Z")

A DPLL(T) Theory solver for Strings [Liang et al CAV 2014]

$$x="abc" \cdot y |y|=4 x="b" \cdot z String solver \rightarrow x\neq"abc" \cdot y \lor x\neq"b" \cdot z Conflict Clause$$

- A theory solver for a core theory of strings with concatenation and length
- Design a theory solver that is:
 - **Refutation and model sound** ("unsat" and "sat" can be trusted)
 - Not terminating in general
 - Efficient in practice

- Support *extended* string functions commonly used in applications
- For example: ctn(x, "c") denotes x contains the substring "c"



Alternatively: use context-dependent simplification:
 x="ab" · y ∧ y="c" | x="abc"

$$x="ab" \cdot y$$

$$y="c"$$

$$\neg ctn(x,"c")$$

$$f(x,"c")$$

$$x\neq"ab" \cdot y \lor y\neq"c" \lor$$

$$ctn(x,"c")$$

Conflict Clause

• Alternatively: use *context-dependent* simplification:

$$x=$$
"ab" $\cdot y \land y=$ "c" $= x=$ "abc"

• Thus:

 $\neg ctn(x, c'') \{x \rightarrow abc''\} \Leftrightarrow \neg ctn(abc'', c'') \Leftrightarrow \bot$

By substitution

By rewriting

Recent Developments for Theory of Strings

- Context-dependent simplifications:
 - Highly aggressive rewrite techniques for strings [Reynolds et al CAV 2019]
 - Applied eagerly, integrated with equality engine [Noetzli et al CAV 2022]
- Reduction lemmas:
 - Improved encodings, witness sharing [Reynolds et al FMCAD 2020]
 - Model-based reductions [Noetzli et al CAV 2022]
- Broadening the core theory of strings:
 - String-to-code point (code) conversions [Reynolds et al IJCAR 2020]
 - Theory of sequences, support for nth and update [Sheng et al IJCAR 2022]

Designing Efficient Theory Solvers

- Use of standard engine for equality reasoning
- Cooperation with other theories
- Fast conflicts, context-dependent simplifications
- Lazy dependence upon expensive reasoning, e.g. reductions
- Other features not mentioned:
 - Proof support

Future Directions in cvc5

Advanced Architectures in cvc5

• What if we used the CDCL(T) engine as a black box?



Advanced Architectures in cvc5

• What if we used the CDCL(T) engine as a black box?



Advanced Architecture: Portfolio



Advanced Architecture: Parallel



Advanced Architecture: Deep Restarts

• Idea: Restart after learning a set of literals that are implied by ${\rm F}$



Deep Restarts

- Given input formula ${\rm F}$
 - A learnable literal 1 is:
 - Meets some syntactic criteria, e.g. ${\tt l}$ is a literal from ${\tt F}$
 - F **|**_T 1
 - Can instrument the SAT solver to record learned literals
 - Literals $\ensuremath{\mathbbmll}$ that are propagated at decision level zero
- A strategy for deep restarts:
 - The solver has learned at least one literal
 - No literal has been learned after some threshold (based on size of F)
- Learned literals may drastically impact preprocessing



Deep Restarts

- Possible variants:
 - In-processing: maintain SAT solver state?
 - Preprocessing changes mapping from SAT to theory literals
 - Restart while saving certain theory lemmas?
 - Based on usefulness criteria
 - Save to disk and restart later?

Difficulty Estimation

• When cvc5 can't solve an input, can we estimate *why* it was difficult?



Difficulty Estimation

- Given input ${\rm F_1} \wedge ... \wedge {\rm F_n}$
 - Model-based:
 - When a candidate model ${\ensuremath{\mathbb M}}$ is constructed
 - Increment difficulty measure for each \mathbb{F}_{ij} that \mathbb{M} does not satisfy
 - Conflict-based:
 - When a conflict clause ($l_1 \lor ... \lor l_n$) is raised
 - For each literal l_i , increment difficulty measure for the F_j s.t. $F_j \models \neg l_i$



• Thanks for listening!

