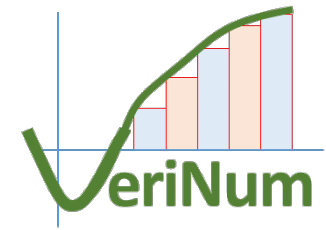
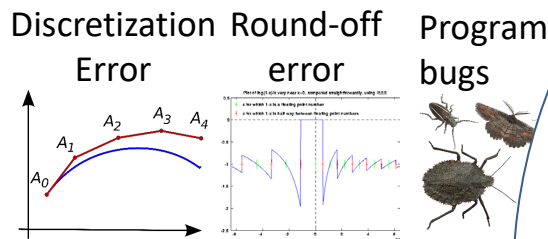


# Formally Verified Numerical Methods



## Challenge:



mathematical  
problem spec.

domain-specific mathematics

$\mathbb{R}$  functional model

LAProof  
library

VCFloat  
tool

• • •

$\mathbb{F}$  functional model

Verified  
Software  
Toolchain

Sparse  
matrix  
library

C program

## Solution:

- End-to-end proofs in Coq
- Layered & modular
- New libraries, new tools, analysis algorithms

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CCF-2219758 Cornell University, David Bindel

## Scientific Impact:

- Connect the mathematical theory of numerical analysis to machine-checked formal methods.
- Demonstrate layered modular approach to formal-methods community
- Validate results and methods in computational science

## Broader Impact and Broader Participation:

- Primary impact: scientific/engineering computation
- Transition to practice: verified libraries
- Outreach: invited talk at 2025 International Workshop on Verification of Scientific Software

